SOME LOCAL AND GLOBAL PROPERTIES OF VISCOSITY SOLUTIONS OF ELLIPTIC PDE'S

I. CAPUZZO DOLCETTA (UNIVERSITÀ ROMA "LA SAPIENZA", ITALY)

ABSTRACT. The aim of the talk is to present some recent results, in collaboration with A. Vitolo (Università di Salerno), concerning viscosity solutions of fully nonlinear elliptic equations of the form $(E)F(x, u(x), Du(x), D^2u(x)) = 0.$

The issues touched are the validity under quite general structure conditions on F of the Alexandrov-Bakelman-Pucci estimate, the boundary weak Harnack inequality and the Krylov-Safonov Growth Lemma.

These tools allow to establish the Weak Maximum Principle for bounded viscosity solutions of equations (E) in general unbounded domains as well as some qualitative Phragmen-Lindelof type theorems.